

Solution to Homework 2: LL(1) parsing

In order for the grammar to parse the terminal symbols in the correct order, we introduce new non-terminals and produce the following grammar:

Grammar (1)

S ::= Exp \$

Exp ::= Exp || AndAnd
| AndAnd

AndAnd ::= AndAnd && Or
| Or

Or ::= Or | And
| And

And ::= And & Not
| Not

Not ::= ! Not
| Unit

Unit ::= true
| false

Our next step would be to eliminate the left recursion which the LL(1) parser can not handle, so we produce our final grammar(2):

Grammar (2)

S ::= Exp \$

Exp ::= AndAnd Exp'
Exp' ::= || AndAnd Exp'
| ϵ

AndAnd ::= Or AndAnd'
AndAnd' := && Or AndAnd'
| ϵ

Or ::= And Or'
Or' ::= | And Or'
| ϵ

And ::= Not And'
And' := & Not And'
| ϵ

Not ::= ! Not
| Unit

Unit ::= true
| false

The next step in the creation of an LL(1) parser is to calculate the FIRST and FOLLOW sets:

Non-terminal	Nullable	FIRST	FOLLOW
S		!, true, false	
Exp		!, true, false	\$
Exp'	Yes	, ε	\$
AndAnd		!, true, false	, \$
AndAnd'	Yes	&&, ε	, \$
Or		!, true, false	&&, , \$
Or'	Yes	, ε	&&, , \$
And		!, true, false	, &&, , \$
And'	Yes	&, ε	, &&, , \$
Not		!, true, false	&, , &&, , \$
Unit		true, false	&, , &&, , \$

Now we are ready to construct the *predictive parsing table*

	!	&		&&		true	False	\$
S	S->Exp \$					S->Exp \$	S->Exp \$	
Exp	Exp -> AndAnd Exp'					Exp -> AndAnd Exp'	Exp -> AndAnd Exp'	
Exp'					Exp'-> AndAnd Exp'			Exp->ε
AndAnd	AndAnd-> Or AndAnd'					AndAnd-> Or AndAnd'	AndAnd-> Or AndAnd'	
AndAnd'				AndAnd'-> && Or AndAnd'	AndAnd'->ε			AndAnd'-> ε
Or	Or->And Or'					Or->And Or'	Or->And Or'	
Or'			Or'-> And Or'	Or'->ε	Or'->ε			Or'->ε
And	And-> Not And'					And-> Not And'	And-> Not And'	
And'		And'-> & Not And'	And'->ε	And'->ε	And'->ε			And'->ε
Not	Not->! Not					Not -> Unit	Not -> Unit	
Unit						Unit-> true	Unit->false	

What is left is just to code the above table in a LL(1) parser